



AN APPROACH TO LUT BASED MULTIPLIER FOR SHORT WORD LENGTH DSP SYSTEMS

NAKKA VENKATA SASI PRIYA*1, Mr. K. V. HAREESH*2, GAJJALA SUVARNA*3, SHAIK SULTHAN BI*4, SHAIK RESHMA*5

ABSTRACT:

Recently, we have proposed the antisymmetric product coding (APC) and odd-multiple-storage (OMS) techniques for lookup-table (LUT) design for memory-based multipliers to be used in digital signal processing applications. Each of these techniques results in the reduction of the LUT size by a factor of two. In this brief, we present a different form of APC and a modified OMS scheme, in order to combine them for efficient memory-based multiplication. The proposed combined approach provides a reduction in LUT size to one-fourth of the conventional LUT. We have also suggested a simple technique for selective sign reversal to be used in the proposed design. It is shown that the proposed LUT design for small input sizes can be used for efficient implementation of high-precision multiplication by input operand decomposition. It is found that the proposed LUT-based multiplier involves comparable area and time complexity for a word size of 8 bits, but for higher word sizes, it involves significantly less area and less multiplication time than the canonical-signed-digit (CSD)-based multipliers

1. INTRODUCTION

Along with the device scaling over the years, semiconductor memory has become cheaper, faster and more power-efficient. Moreover, according to the projections of the ITRS embedded memories will have dominating presence in the SoC, which may exceed 90% of total SoC content. It has also been found that the transistor packing density memory components is not only high but also increasing much faster than the transistor density of logic components. Apart from that, the memory-based computing structures are more regular than the multiply-accumulate structures; and offer many other advantages, e.g., greater potential for high throughput and low-latency implementation; and less dynamic power consumption. Memorybased computing is well-suited for many DSP

algorithms, which involve multiplication with fixed set of coefficients. The basic functional model of memory-based multiplier is shown in Fig.1.1. Let A be a fixed coefficient and X be an input word to be multiplied with A. Assuming X to be a positive binary number with word-length L, there can be 2L possible values of X, and accordingly, there can be 2L possible values of product $C = A \cdot X$. Therefore, for memory based multiplication, an LUT of 2L words consisting of precomputed product values corresponding to all possible values of X is conventionally used. The product-word A·Xi is stored at the location whose address is the same as Xi for $0 \le 2L-1$, such that if L-bit binary value of Xi is used as address for the LUT, then the corresponding product value A·Xi is available as its output.

* 1,3,4,5 B. Tech Students, *2 Assistant Professor, Dept. of Electronics and Communication Engineering, RISE Krishna Sai Prakasam Group of Institutions

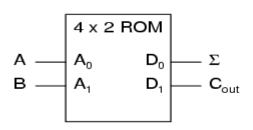


Several architectures have been reported the literature for memory-based in Implementation of DSP algorithms involving orthogonal transforms and digital filters but do not find any significant work on LUT optimization for memory based multiplication. A new approach to LUT design for memorybased multiplication, which could be used to reduce the memory-size by half for small inputwidths. It is shown that although 2L possible values of X correspond to 2L possible values of C = A.X, only (2L/2) words corresponding to the odd multiples of A may only be stored in the LUT while the even multiples of A could be derived by left-shift operations of one of those odd multiples. Using this approach, one can reduce the LUT size to half, but it has significant combinational overhead since it requires a barrel-shifter along with a control-circuit to generate the control-bits for producing a maximum of (L-1) left-shifts, and an encoder to map the L-bit input word to (L - 1)-bit LUT address. In this project, two new schemes are proposed for optimization of LUT with lower area- and time-overhead. One of the proposed optimization is based on exclusion of sign-bit from the LUT address, and the other optimization is based on a recoding of stored product word.

General LUT Design

It is possible to store binary data within solid-state devices. Those storage "cells" within solid-state memory devices are easily addressed by driving the "address" lines of the device with the proper binary values. A ROM memory circuit written, or programmed, with certain data, such that the address lines of the ROM served as inputs and the data lines of the ROM served as outputs, generating the characteristic response of a particular logic function. Theoretically, could ROM chip can program to emulate whatever logic function, wanted without having to alter any wire connections or gates.

Consider the following example of a 4 x 2 bit ROM memory programmed with the functionality of a half adder:



Α	Address		Data	
	Α	В	Cout	Σ
	0	0	0	0
	0	1	0	1
	1	0	0	1
	1	1	1	0

4X2 ROM

If this ROM has been written with the above data representing a half-adder's truth table, driving the A and B address inputs will cause the respective memory cells in the ROM chip to be enabled, thus outputting the corresponding data as the Σ (Sum) and C out bits. Unlike the half-adder circuit built of gates or relays, this device can be set up to perform any logic function at all with two inputs and two

outputs, not just the half-adder function. To change the logic function, all we would need to do is write a different table of data to another ROM chip. EPROM chip can also program which could be re-written at will, giving the ultimate flexibility in function.

It is vitally important to recognize the significance of this principle as applied to digital



circuitry. Whereas the half-adder built from gates or relays processes the input bits to arrive at a specific output, the ROM simply remembers what the outputs should be for any given combination of inputs. This is not much different from the "times tables" memorized in grade school: rather than having to calculate the product of 5 times 6(5+5+5+5+5+5=30), school-children are taught to remember that $5 \times 6 = 30$, and then expected to recall this product from memory as needed. Likewise, rather than the logic function depending on the functional arrangement of hard-wired gates or relays (hardware), it depends solely on the data written into the memory (software).

Such a simple application, with definite outputs for every input, is called a look-up table, because the memory device simply "looks up" what the outputs should to be for any given combination of inputs states.

This application of a memory device to perform logical functions is significant for several reasons:

- Software is much easier to change than hardware.
- Software can be archived on various kinds of memory media (disk, tape), thus providing an easy way to document and manipulate the function in a "virtual" form; hardware can only be "archived" abstractly in the form of some kind of graphical drawing.
- Software can be copied from one memory device (such as the EPROM chip) to another, allowing the ability for one device to "learn" its function from another device.
- Software such as the logic function example can be designed to perform functions that would be extremely difficult to emulate with discrete logic gates.

The usefulness of a look-up table becomes more and more evident with increasing complexity of function. To build a 4-bit adder circuit using a ROM, A ROM is required with 8 address lines and 4 data lines.

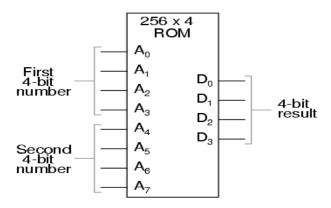


Figure 1. 256X4 ROM

Devices such as this, which can perform a variety of arithmetical tasks as dictated by a binary input code, are known as Arithmetic Logic Units, and they comprise one of the essential components of computer technology.

Although modern ALUs are more often constructed from very complex combinational logic circuits for reasons of speed, it should be comforting to know that the exact same functionality may be duplicated with a "dumb"



ROM chip programmed with the appropriate look-up table. In fact, this exact approach was used by IBM engineers in 1959 with the development of the IBM 1401 and 1620 computers, which used look-up tables to perform addition, rather than binary adder circuitry. The machine was fondly known as the "CADET," which stood for "Can't Add, Doesn't Even Try."

2. LITERATURE SURVEY

The efficient memory-based VLSI array designs for DFT and DCT

Guo, J.-I.; Liu, C.-M.; Jen, C.-W Nat. Chiao Tung Univ., Hsinchu

Efficient memory-based VLSI arrays and a new design approach for the discrete Fourier transform and discrete cosine transform are presented. The DFT and DCT are formulated as cyclic convolution forms and mapped into linear arrays which characterize small numbers of I/O channels and low I/O bandwidth. Since the multipliers consume much hardware area, the designs utilize small ROMs and adders to implement the multiplications. Moreover, the ROM size can be reduced effectively by arranging the data in the designs appropriately. The arrays outperform others in the architectural topology computing speeds, complexity, the number of I/O channels, and I/O bandwidth. They benefit from the advantages of both systolic array and the memory-based architectures

On the design automation of the memorybased VLSI architectures for FIR filters

Lee, H.-R. Jen, C.-W. Liu, C.-M. Dept. of Electron. Eng., Nat. Chiao Tung Univ., Hsinchu An approach to automating the design of memory-based VLSI architectures for FIR filters has been developed. The automation is based on the exploration of the design space and

schemes for efficient memory replacement, algorithm formulation, architecture design, and evaluation method. Various schemes and design considerations were integrated to produce a parameterized memory-based architecture that can easily be tuned to various hardware-speed requirements. This MBA is characterized by three design parameters. Differently configured MBAs result from specifying different values for these parameters. Hardware-speed evaluation formulas were established based on the required elements in MBAs. These elements include ROM, adders, and shift registers. These formulas and a cell library of a target technology can be used to design an optimally configured MBA by searching for the best values of the design parameters with the aid of a computer. Using the evaluation formulas and the parameterized architecture, an area-minimized architecture can be synthesized under a speed specification. Based on these results, automatic synthesis too has been developed

A memory-efficient realization of cyclic convolution and its application to discrete cosine transform

The memory efficient design for realizing the cyclic convolution and its application to the discrete cosine transform. To adopt the method of distributed arithmetic computation, and exploit the symmetry property of DCT coefficients to merge the elements in the matrix of the DCT kernel and then separate the kernel to be two perfect cyclic forms to facilitate an efficient realization of 1-D N-point DCT using (N-1)/2 adders or subtractors, one small ROM module, a barrel shifter, and N-1/2+1 accumulators. The comparison results with the existing designs show that the proposed design can reduce delay-area product significantly.



Memory-based hardware for resourceconstraint digital signal processing systems

The current trends of advancement of memory technology indicates reasonable scope to have efficient memory-based computing systems as promising alternative to the conventional logic-only computing in order to meet the stringent constraints and growing requirements of the digital signal processing systems in widely varying application environments. Several algorithms architectures have been proposed in the literature to reduce the area- and timecomplexities of commonly encountered computation-intensive cores of DSP functions by memory-based computing, but many more novel algorithms and architectures need to be developed to design flexible area-delay-powerefficient systems for various DSP applications.

3. EXISTING SYSTEM

A conventional LUT based multiplier is shown in Fig.1.1, where A is a fixed coefficient, and X is an input word to be multiplied with A. Assuming X to be a positive binary number of word length L, there can be 2L possible values of X, and accordingly, there can be 2L possible values of product $C = A \cdot X$. Therefore, for memory-based multiplication, an LUT of 2L words, consisting of pre-computed product values corresponding to all possible values of X, is conventionally used. The product word A · Xi is stored at the location Xi for $0 \le Xi \le 2L - 1$, such that if an L-bit binary value of Xi is used as the address for the LUT, then the corresponding product value A · Xi is available as its output. Several architectures have been reported in the literature for memory-based implementation of DSP algorithms involving orthogonal transforms and digital filters.

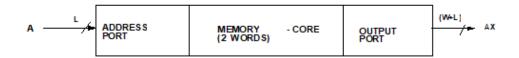


Fig 2. Conventional LUT Multiplier

- If the input bit size is 5 bits then the memory stores all the 2^5 possible Outcomes which results in increase in LUT size. If the bits increase then the LUT Size increases exponentially
- Several architectures have been reported in the literature for memory-based implementation of DSP algorithms involving orthogonal transforms and digital filters .However, it is not found any significant work on LUT

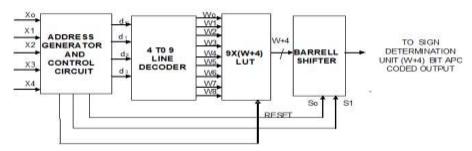
optimization for memory-based multiplication.

4. PROPOSED SYSTEM ARCHITECTURE

A new approach to LUT design is presented, where only the odd multiples of the fixed coefficient are required to be stored, which is referred to as the odd-multiple-storage scheme in this brief. In addition, we have shown that, by the anti-symmetric product coding approach, the LUT size can also be reduced to half, where the



product words are recoded as Anti-symmetric



pairs.

Fig 3. Proposed LUT Multiplier

if the input bit size= 5 then the memory stored is of $2^5/2 = 15$ locations which results in a reduction in LUT size by factor of 2.

Objective

To build an LUT multiplier and the improvement is regarding the area consumption which increases exponentially in the existing LUT multipliers. Comparison of existing Booth multiplier with proposed LUT multiplier.

5. THE DESIGN FLOW

This section examines the flow for design using FPGA. This is the entire process for designing a device that guarantees that will not overlook any steps and that will have the best chance of getting backs a working prototype that functions correctly in the system.

The design flow consists of the steps in

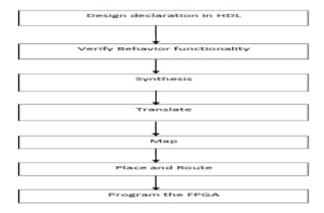


Figure.5. FPGA Design Flow

Design Entity

The basic architecture of the LUT is designed in this step which is coded in VHDL.



Behavioral Simulation

After the design phase, the LUT is verified using simulation software i.e. Xilinx ISE Simulator for different inputs to generate outputs and if it verifies then proceed further otherwise modification and necessary correction will be done in the HDL code. This is called as the behavioral simulation. Simulation is an ongoing process while the design is being done. Small sections of the design should be simulated separately before hooking them up to larger sections. There will be much iteration of design and simulation in order to get the correct functionality. Once design and simulation are finished, another design review must take place so that the design can be checked. It is important to get others to look over the simulations and make sure that nothing was missed and that no improper assumption was made. This is one of the most important reviews because it is only with correct and complete simulations that verify whether this chip will work correctly in the required system.

Proposed LUT APC Part

The structure and function of the LUT-based multiplier for L=5 using the APC technique is shown in Fig.3.2 It consists of a four-input LUT of 16 words to store the APC values of product words as given in the sixth column of Table I, except on the last row, where 2A is stored for input X=(00000) instead of storing a "0" for input X=(10000). Besides, it consists of an address-mapping circuit and an add/subtract circuit. The address-mapping circuit generates the desired address (x3', x2', x1', x0'). A straightforward implementation of address mapping can be done by X'L using x4 as the control bit. The address-mapping circuit, however, can be optimized to be realized by three XOR gates, three AND gates, two OR gates, and a NOT gate, as shown in Fig. 3.2 Note that the RESET can be generated by a control circuit (not shown in this figure) .The output of the LUT is added with or subtracted from 16A, for x4=1 or 0, respectively, by the add/subtract cell. Hence, x4 is used as the control for the add/subtract cell.

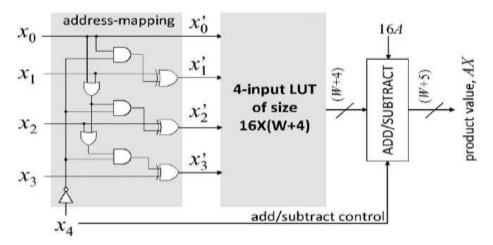


Figure 6. Proposed APC Part

For simplicity of presentation, it is assumed both X and A to be positive integers. The product words for different values of X for L=5 are shown in Table I. It may be observed in this table that the input word X on the first column of each row is the two's complement of that on the third column of the same row. In addition, the sum of product values corresponding to these two input values on the same row is 32A. LUT based multiplier for L=5 using the APC technique



W = Width of A

L = Width of X

Table 1: Stored APC Words

APC Words for Different Input Values for L=5

Input, X	product values	Input, X	product values	address $x_3'x_2'x_1'x_0'$	APC words
00001	A	11111	31A	1 1 1 1	15A
00010	2A	11110	30A	1 1 1 0	14A
00011	3A	11101	29A	1 1 0 1	13A
00100	4A	11100	28A	1 1 0 0	12A
00101	5 <i>A</i>	11011	27A	1 0 1 1	11A
00110	6A	11010	26A	1 0 1 0	10A
00111	7A	11001	25A	1 0 0 1	9A
01000	8 <i>A</i>	11000	24A	1 0 0 0	8A
01001	9A	10111	23A	0 1 1 1	7A
01010	10A	10110	22A	0 1 1 0	6A
01011	11A	10101	21A	0 1 0 1	5A
01100	12A	10100	20A	0 1 0 0	4A
01101	13A	10011	19A	0 0 1 1	3A
01110	14A	10010	18A	0 0 1 0	2A
01111	15A	10001	17A	0 0 0 1	A
10000	16A	10000	16A	0 0 0 0	0

For $X = (0\ 0\ 0\ 0\ 0)$, the encoded word to be stored is 16A.

 $16 \times (W+4) \rightarrow 16$ Locations and each location having (W+4) bits.

. Let the product values on the second and fourth columns of a row be u and v, respectively. Since one can write

$$u = [(u+v)/2 - (v-u)/2] \text{ and}$$

$$v = [(u+v)/2 + (v-u)/2], \text{ for } (u+v) = 32A,$$

$$U=16A+\lceil (V-U)/2 \rceil \qquad \qquad V=16A-\lceil (V-U)/2 \rceil$$

The product values on the second and fourth columns of Table I therefore have a negative mirror symmetry. This behavior of the product words can be used to reduce the LUT size, where, instead of storing u and v, only [(v-u)/2] is stored for a pair of input on a given row. The 4-bit LUT addresses and corresponding coded words are listed on the fifth and sixth columns of the table, respectively. Since the representation of the product is derived from the antisymmetric behavior of the products, we can name it as antisymmetric product code. The 4-bit address $X_{-}=(x_{-}3,x_{-}2,x_{-}1,x_{-}0)$ of the APC word is given by



Flow Chart For Proposed APC Part

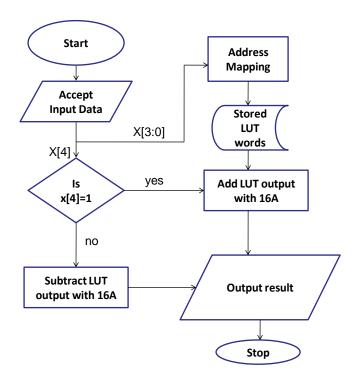


Figure.7. Flow Chart for Proposed LUT

Proposed APC-OMS Part

For the multiplication of any binary word X of size L, with a fixed coefficient A, instead of storing all the 2L possible values of $C = A \cdot X$, only (2L/2) words corresponding to the odd multiples of A may be stored in the LUT, while all the even multiples of A could be derived by left-shift operations of one of those odd multiples. Based on the above assumptions, the LUT for the multiplication of an L-bit input with a W-bit coefficient could be designed by the following strategy.

- 1) A memory unit of [(2L/2) + 1] words of (W + L)-bit width is used to store the product values, where the first (2L/2) words are odd multiples of A, and the last word is zero.
- 2) A barrel shifter for producing a maximum of (L-1) left shifts is used to derive all the even multiples of A.
- 3) The L-bit input word is mapped to the (L 1)-bit address of the LUT by an address encoder, and control bits for the barrel shifter are derived by a control circuit.



input X' $x'_3x'_2x'_1x'_0$	product value	# of shifts	shifted input, $X^{\prime\prime}$	stored APC word	address $d_3d_2d_1d_0$
0 0 0 1	A	-0			
0 0 1 0	$2 \times A$	1.	0 0 0 1	P0 = A	0 0 0 0
0 1 0 0	$4 \times A$	2	0001	10=21	0000
1 0 0 0	$8 \times A$	3			
0 0 1 1	3.4	-0			
0 1 1 0	2×3.4	1	0 0 1 1	P1 = 3A	0001
1 1 0 0	$4 \times 3A$	2			
0 1 0 1	5.4	-0	0101	P2 = 5A	0010
1 0 1 0	$2 \times 5A$	1	0.10.1		
0 1 1 1	7.4	0	0111	P3 = 7A	0011
1 1 1 0	$2 \times 7A$	1	0111	2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 -	0.011
1 0 0 1	9.4	-0	1001	P4 = 9A	0 1 0 0
1 0 1 1	11.4	-0	1 0 1 1	P5 = 11A	0 1 0 1
1 1 0 1	13.4	0	1 1 0 1	P6 = 13A	0 1 1 0
1 1 1 1	15A	-0	1 1 1 1	P7 = 15A	0 1 1 1

Table 2: Stored APC-OMS Words

Control Circuit

The control bits s0 and s1 to be used by the barrel shifter to produce the desired number of shifts of the LUT output are generated by the control circuit, according to the relations

$$s_0 = \overline{x_0 + \overline{(x_1 + \overline{x_2})}}$$

$$s_1 = \overline{(x_0 + x_1)}.$$

Note that (s1s0) is a 2-bit binary equivalent of the required number of shifts specified in Tables II. The RESET signal can alternatively be generated as (d3 AND x4).

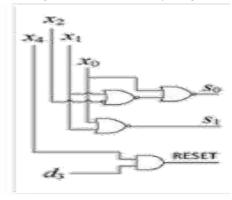


Figure 3.6 Control Circuit For Generation Of S0, S1, And Reset



The control circuit to generate the control word and RESET is shown in Fig. 3.7.The address-generator circuit receives the 5-bit input operand *X* and maps that onto the 4-bit address word (d3d2d1d0)

6. SIMULATION RESULTS & SYNTHESIS REPORTS

APC

Address Mapping

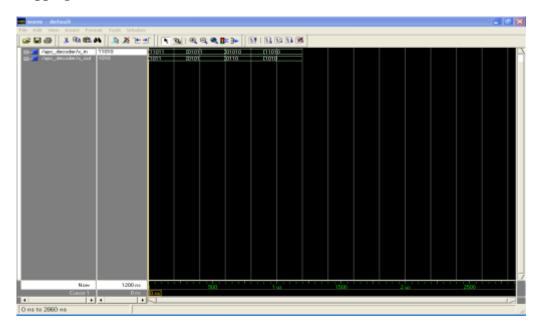


Figure 6.1 Simulation result of Address Mapping Unit

Address mapping unit converts the input to either two complement output or the input by seeing the LSB of the input

6.2. LUT APC



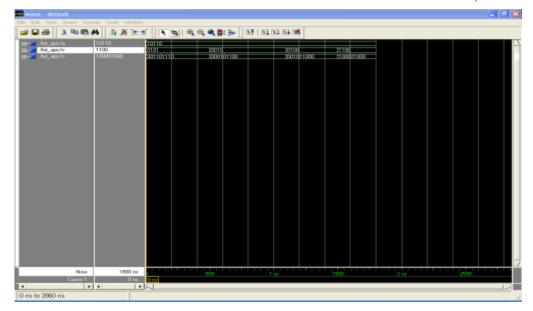


Figure 6.2 Simulation result of LUT APC Unit

LUT stores APC product word.

6.3. Add Sub Unit

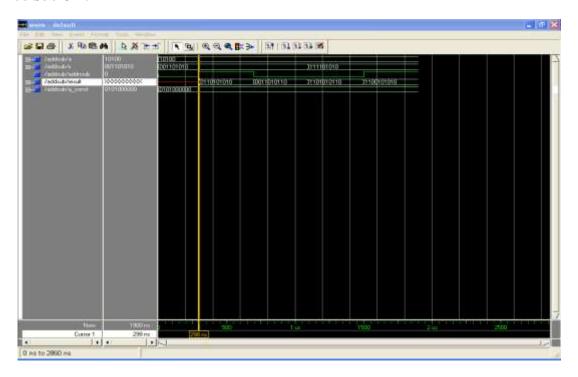


Figure 6.3 Simulation result of ADD SUB Unit

Add Sub unit either Add or Sub with 16A according to the value of the MSB of input

6.4.LUT APC Top Module



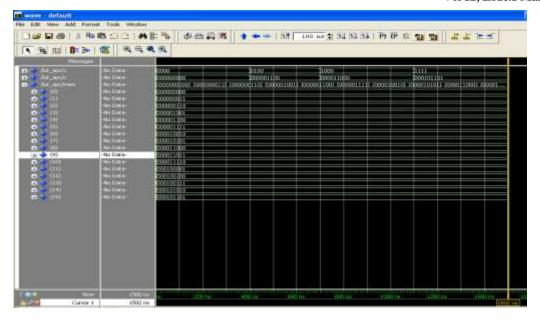


Figure 6.4 Simulation result of LUT APC Top Module

Output is equal to A.X and this module combines all the above three modules when A as constant

6.5. OMS

Address Generation

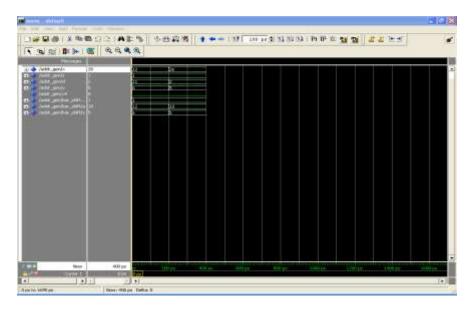


Figure 6.5 Simulation result of Address Generation Unit

6.6. Control Circuit



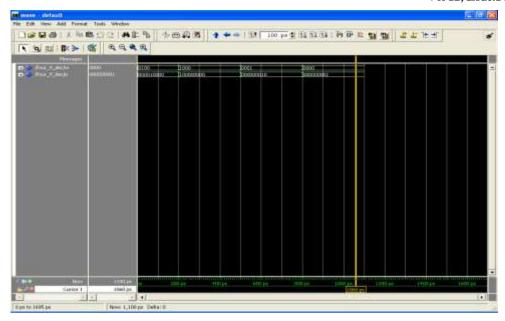


Figure 6.6 Simulation Result Of Control Circuit Unit

6.7. LUT APC & OMS

With A = 20

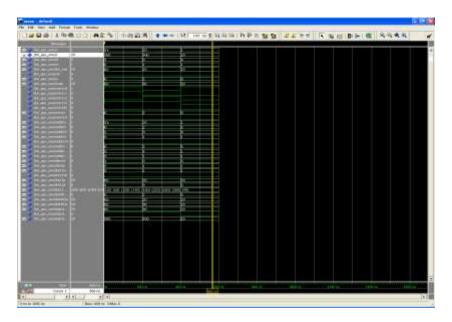


Fig 6.7 Simulation result of LUT APC & OMS Unit

6.8.FIR Filter With LUT



LUT With Constants {9, 17,13,1}

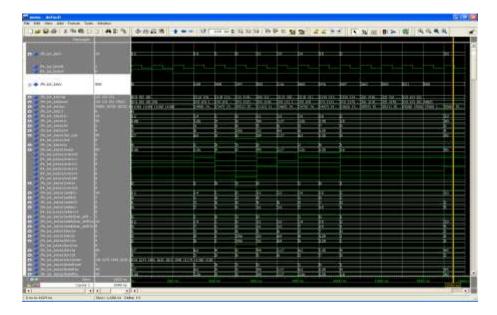


Fig. 6.8. Simulation result of FIR Filter with LUT of Constants {9, 17,13, 1}

6.9. LUT 3 With Third Constant

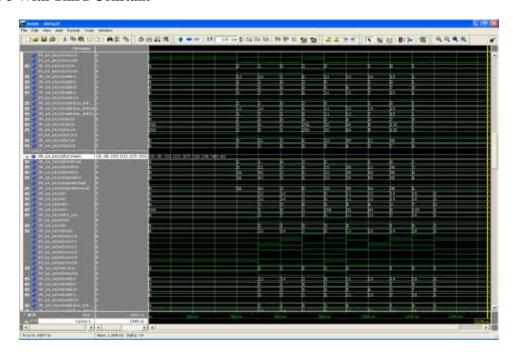


Fig 6.9. Simulation result of LUT 3 with Third Constant

6.10. LUT 4 With Fourth Constant



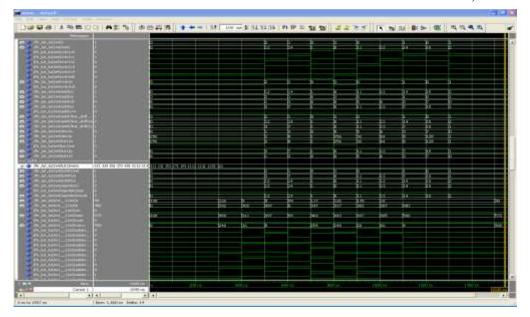


Fig 6.10. Simulation result of LUT 4 with Fourth Constant

Xilinx Synthesis Blocks

LUT APC



Fig 6.11 Top level View of LUT APC-OMS Circit

Interior Diagram



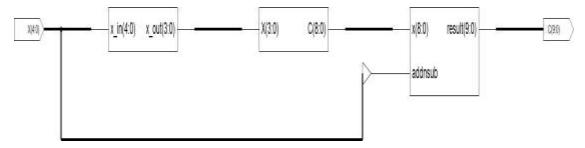


Fig .6.12.Interior diagram of LUT APC-OMS Unit

Add / Sub Unit

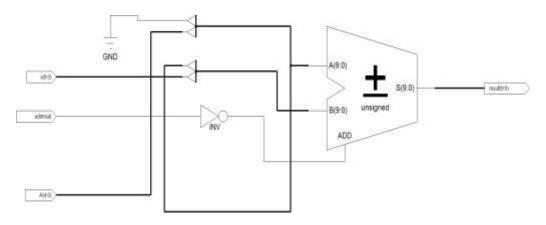


Fig 6.13. Add / Sub Unit

Address Generate unit

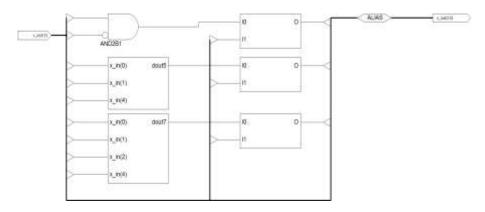


Fig 6.14.Address Generate unit

LUT Unit



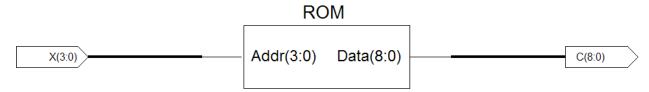


Fig 6.15. LUT Unit

6.11. Comparision Between The Synthesis Results Of FIR Filter With BOOTH MItiplier & FIR Filter With LUT Multiplier

Table .1 Synthesis Result Of FIR Filter With BOOTH Multiplier

NUMBER OF SLICES	87 OUT 0F 4656
NUMBER OF SLICE FLIP FLOPS	24 OUT OF 9312
NUMBER OF 4 INPUT LUTS	149 OUT OF 9312
NUMBER OF GATED CLOCKS	01 OUT OF 24

Table .2 Synthesis Result Of FIR Filter With LUT Multiplier

NUMBER OF SLICES	35 OUT 0F 4656
NUMBER OF SLICE FLIP FLOPS	24 OUT OF 9312
NUMBER OF 4 INPUT LUTS	62 OUT OF 9312
NUMBER OF GATED CLOCKS	01 UT OF 24

7.CONCLUSION & FUTURE SCOPE

It is found that the proposed LUT-based multiplier involves comparable area and time complexity for a word size of 8 bits, but for higher word sizes, it involves significantly less area and less multiplication time than the canonical-signed-digit (CSD)-based multipliers.

For 16 and 32 bit word sizes, respectively, it offers more than 30% and 50% of saving in areadelay product over the corresponding CSD multipliers.

The proposed LUT multipliers for word size L = W = 5 bits are coded in VHDL and synthesized by XILINX using the TSMC 90-nm Library, where the LUTs are implemented as arrays of constants. The CSD-based multipliers having the same addition schemes are also synthesized with the same technology library.

8. FUTURE SCOPE

In future this LUT based multipliers can also be used in DSP systems for multiplications involving in FFT . It can be able to give the good results when compared to LUT multipliers using in FIR filters.

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